1. (a) How many lattice paths from $(0,0)$ to $(m, n)$ remain the same when you rotate them by 180 degrees about $\left(\frac{m}{2}, \frac{n}{2}\right)$ ? Prove your answer.
2. (a) How many lattice paths from $(0,0)$ to $(n, n)$ remain the same when you flip them across the diagonal joining $(n, 0)$ and $(0, n)$ ? Prove your answer.
(b) What is the sum of the $q$-weights of these lattice paths? Conjecture an answer.
(c) Why is there no part (b) for question 1?
